

# Financial Mathematics

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<sup>1</sup>Based on Robert L. McDonald's *Derivatives Markets*, 3rd Ed, Pearson, 2013.

# Chapter 1. Introduction to Derivatives

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§ 1.1 What is a derivative?

§ 1.2 An overview of financial markets

§ 1.3 The use of derivatives

§ 1.4 Buying and short-selling financial assets

§ 1.5 Problems

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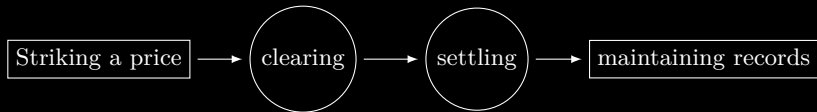
§ 1.3 The use of derivatives

§ 1.4 Buying and short-selling financial assets

§ 1.5 Problems

The trading of a financial asset involves at least four discrete steps:

1. A buyer and a seller must locate one another and agree on a price
2. The trade must be **cleared**  
(the obligations of each party are specified)
3. The trade must be **settled**  
(the buyer and the seller must deliver the cash or securities necessary to satisfy their obligations in the required period of time)
4. Ownership records are updated.



There are at least four different **measures of a market and its activity**:

1. **Trading volume**: the number of financial claims that change hands daily or annually.
2. **Market value or market cap**: the sum of the market value of the claims that **could** be traded, without regard to whether they have traded.
3. **Notional value**: Notional value measure the scale of a position, usually with reference to some underlying asset.
4. **Open Interest**. Open interest measures the total number of contracts for which counter parties have a future obligation to perform. It is an important statistic in derivatives market.

## Companies typically raise funds by

| stock markets  | bound markets   |
|--|---|
| Selling ownership claims<br>Securities exchanges<br>(NYSE, NASDAQ) | Obtaining a bank loan or issuing a bond<br>Through dealers<br><br>less frequent |

The introduction of derivatives in a market often coincides with an increase in price risk in that market. For example,

1. Currencies were permitted to float in 1971 when the gold standard was officially abandoned. The modern market in financial derivatives began in 1972, when the Chicago Mercantile Exchange started trading futures contracts on seven currencies.
2. OPEC's 1973 reduction in the supply of oil was followed by high and variable oil prices.
3. U.S. interest rates became more volatile following inflation and recessions in the 1970s.
4. The market for natural gas has been deregulated gradually since 1978, resulting in a volatile market in recent years.
5. The deregulation of electricity began during the 1990s.



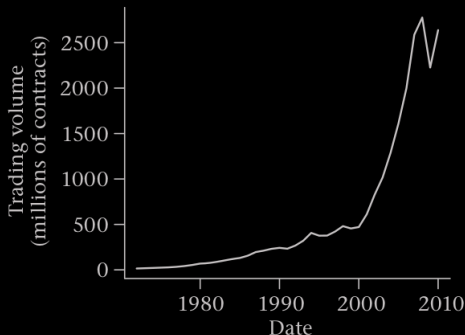
# History of the crude oil prices



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<sup>2</sup>Image from <https://www.macrotrends.net/>

Price variability leads to the development of derivatives markets to efficiently share risk.



Millions of future contracts traded annually at the Chicago Board of Trade (CBT), Chicago Mercantile Exchange (CME), and the New York Mercantile Exchange (NYMEX), 1970-2011.

## Examples of underlying assets on which futures contracts are traded:

| Category         | Description   |
|------------------|---|
| Stock index      | S&P 500 index, Euro Stoxx 50 index, Nikkei 225, Dow-Jones Industrials, Dax, NASDAQ, Russell 2000, S&P Sectors (healthcare, utilities, technology, etc.) |
| Interest rate    | 30-year U.S. Treasury bond, 10-year U.S. Treasury notes, Fed funds rate, Euro-Bund, Euro-Bobl, LIBOR, Euribor   |
| Foreign exchange | Euro, Japanese yen, British pound, Swiss franc, Australian dollar, Canadian dollar, Korean won  |
| Commodity        | Oil, natural gas, gold, copper, aluminum, corn, wheat, lumber, hogs, cattle, milk   |
| Other            | Heating and cooling degree-days, credit, real estate  |

## The role of financial markets

Insurance companies and individual communities/families have traditionally helped each other to share risks.

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Markets make **RISK-SHARING** more efficient

|                                |  |                    |
|--------------------------------|--|--------------------|
| <b>Diversifiable risks</b>     | vanishes   | lightening strike  |
| <b>Non-diversifiable risks</b> | are reallocated to those most willing to hold it | Stock market crash |

The existence of risk-sharing mechanisms benefits everyone!