**Financial Mathematics** 

MATH 5870/6870<sup>1</sup> Fall 2021

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<sup>&</sup>lt;sup>1</sup>Based on Robert L. McDonald's *Derivatives Markets*, 3rd Ed, Pearson, 2013.

# Chapter 2. An Introduction to Forwards and Options

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- § 2.1 Forward contracts
- $\$  2.2 Call options
- § 2.3 Put options
- § 2.4 Options are insurance
- § 2.5 Summary of forward and option positions
- 2.6 Problems

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Call option : Buyer can walk away.

???? option : Seller can walk away.

**Definition 2.3-1** A put option gives the owner the right but not the obligation to sell the underlying asset at a predetermined price during a predetermined time period.

Remark 2.3-1 Similar to the call option case, a premium paid by the put buyer at the time the option is purchased is needed in order to compensate the put seller for being in a disadvantage position.

of put option	someone needs to		premium
seller	buy	has to buy if asked	receive
buyer	sell	can walk away	pay

Payoff of purchased put = max (0, strike price - spot price at expiration)

Profit of purchased put = payoff of purchased put - future value of option premium

Payoff of written put = -max(0, strike price - spot price at expiration)

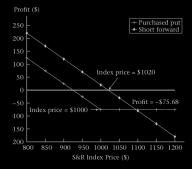
Profit of written put = payoff of written put + future value of option premium Example 2.3-1 S&R Index 6-month European put option

Strike price = \$1,000, Premium = \$74.20, 6-month risk-free rate = 2%.

Compute both payoff and profit of the purchased put option if the index value in six months \$1, 100 (resp. \$900).

#### Solution.

If index value in six months = \$1,100, Payoff = max(0, \$1,000 - \$1,100)= \$0 Profit = \$0 - \$74.20 × 1.02 = -\$75.68. If index value in six months = \$900, Payoff = max(0, \$1, 000 - \$900)= \$100Profit =  $\$100 - \$74.20 \times 1.02$ = \$24.32.



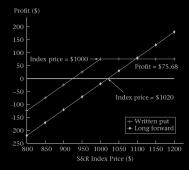
Example 2.3-2 S&R Index 6-month European put option

Strike price = \$1,000, Premium = \$74.20, 6-month risk-free rate = 2%.

Compute both payoff and profit of the written put option if the index value in six months \$1, 100 (resp. \$900).

#### Solution.

If index value in six months = \$1,100, Payoff =  $-\max(0, \$1, 000 - \$1, 100)$ = \$0Profit =  $\$0 + \$74.20 \times 1.02$ = \$75.68. If index value in six months = \$900, Payoff =  $-\max(0, \$1, 000 - \$900)$ = -\$100Profit =  $-\$100 + \$74.20 \times 1.02$ = -\$24.32.



A call option becomes more profitable when the underlying asset appreciates in value

A put option becomes more profitable when the underlying asset depreciates in value **Definition 2.3-2 Moneyness** of an option describes whether the option payoff would be positive if the option were exercised immediately.

In particular, one has

Moneyness	payoff if exercised immediately	
In-the-money option	> 0	
At-the-money option	= 0	
Out-of-the money option	< 0	