## Math 221: LINEAR ALGEBRA

# Chapter 1. Systems of Linear Equations §1-5. Application to Electrical Networks 

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Electrical Networks

## Resistor Networks

## Important Symbols:



Resitance is measured in ohms, $\Omega$. Voltage is measured in volts, V. Current is measured in amps, A.

## Problem

Write an equation for each circuit and solve for each current in the following diagram.


Solution
The equation for the bottom circuit, with current $\mathrm{I}_{1}$ is given by

$$
5 \mathrm{I}_{1}+3 \mathrm{I}_{1}+\mathrm{I}_{1}-\mathrm{I}_{2}=-24
$$

The top left circuit, with current $\mathrm{I}_{2}$ is

$$
\mathrm{I}_{2}-\mathrm{I}_{1}+4 \mathrm{I}_{2}-4 \mathrm{I}_{3}+2 \mathrm{I}_{2}=17
$$

The top right circuit is

$$
4 \mathrm{I}_{3}-4 \mathrm{I}_{2}+2 \mathrm{I}_{3}+2 \mathrm{I}_{3}=-14
$$

After simplifying, this system is represented by

$$
\left[\begin{array}{rrr|r}
9 & -1 & 0 & -24 \\
-1 & 7 & -4 & 17 \\
0 & -4 & 8 & -14
\end{array}\right]
$$

Solution (continued)
The reduced row-echelon form of this matrix is

$$
\left[\begin{array}{lll|r}
1 & 0 & 0 & -\frac{5}{2} \\
0 & 1 & 0 & \frac{3}{2} \\
0 & 0 & 1 & -1
\end{array}\right]
$$

This gives values of the currents of

$$
\begin{aligned}
& \mathrm{I}_{1}=-\frac{5}{2} \\
& \mathrm{I}_{2}=\frac{3}{2} \\
& \mathrm{I}_{3}=-1
\end{aligned}
$$

